1. Introduction

Most likely, cigarette smoking is the toxic chemical-exposure in human only most important factor. By the year 2020, the World Health Organization predicts cigarette smoke will lead to killing of approximately 10 million people per year internationally [1]. More than 6000 compounds have been distinguished in cigarette smoke so far [2]; probably, at least 69 of which are known as carcinogens for humankind [3]. In addition, the food and drug administration (FDA) [4] listed cigarette smoke constituents which are potentially harmful. Smoking results in potential threat to the respiratory tract where roughly half of all cigarette smoking related health impacts materialize. Cigarette smoke is a complex mixture of gaseous compounds. Current literature shows 4800 known gases in cigarette smoke. Cigarette smoking is a complicated aggregation of particulate phase and liquid droplets which suspend in a mixture of gases and vapors. The droplets range in different mean diameter (dp < 100 nm) [6] and the toxic agents are dissolved in both vapors and droplets [5]. Cigarette smoking leads to various kinds of illnesses such as primarily lung tumors and asthma, deficiencies of the respiratory organs [7]. Particularly, two potential deadly resultes are lung cancer and chronic obstructive pulmonary disease (COPD) [8].

The chance of developing lung cancer is increased through being exposed to cigarette smoke illustrated by studies. It is vital to understand the development of particular histologic-type cancers regarding the deposition of carcinogenic particles, which are present in human airway. In this paper, the mass transfer and deposition of cigarette smoke, inside the human airway, are investigated applying the finite element method. The mass transfer and depositions of four types of critical cigarette smoke, namely 1, 3-butadiene, acrolein, acetaldehyde and carbon monoxide (CO), in a complete human-airway model (from mouth to B3 generation), under inhalation conditions, have been simulated. In this study, concentration distribution in inhalation is evaluated. The vapour deposition was modelled with 30 and 80 L.min⁻¹ volumetric flow rates. Therefore, a two-dimensional model of human airway from the mouth to generation B3 was reconstructed. Then, for simulating the mass transfers and deposition fraction, the low-Reynolds-number (LRN) k–ω turbulence equation was used.
deposition fraction in human lungs are directly relevant to the tobacco smoking harmful impact [9]. Moreover, since many inhaled toxic or drug aerosols could partially appear in the form of vapor, human airway validated computer simulation would provide essential data for health and safety modeling. The airflow velocity is often expressed by the Navier-Stokes equations [10]. Navier-Stokes equations have been solved via a complex numerical analysis. Nevertheless, they have been applying a lot nowadays. The reason is that there are a lot of high-performance computers nowadays. An analytical method is achievable to solve the Navier-Stokes equations in some particular conditions [11]. The previous studies have been developed via the turbulent models by some researches [12, 13]. These models were developed to assess the nano-particle distributions in the human airway [7, 14]. The finite element method of analysis have been done already to solve the computational model of heat and mass transfer for nano-particle water vapor of the upper human airway [15]. In this paper, a new model is used to simulate cigarette smoke flow in the total lung airway which consists of the mouth-to-generation B3 pathway (see Figure 1). Furthermore, some species of vital carcinogens in cigarette smoke vapor compounds as the kinds for gas/vapor transport/deposition researches: acrolein; 1, 3-butadiene; acetaldehyde and carbon monoxide. Therefore, they come out at the oral entrance in the gas phase [16]. Thus, this model predicts mass transfer and deposition of cigarette smoke in all over lung. The paper is structured as follows: provides the background information about two-dimensional geometric model of the total lung airway, illustrates the changes in velocity profile for mouth and trachea, describes the mass transfer in human airway and the deposition of nano-particles in the 1~100 nm diameter range, presents the particle deposition fractions under different flow rate and provides the distributions of local Sherwood number for cigarette smoke. The goal of the study was to provide a more accurate description of mainstream smoke properties in the human airway during smoking and the various influences that determine those properties. But, there is not any experimental data to evaluate the simulation results. The results of particle deposition in different flow rates are compared with those reported by Zhang and Kleinstreuer [17]. Finally, the paper will draw some conclusions.

2. Methods

2.1 Background information

A key parameter to assess the effects of inhaled cigarette smoke is the particle deposition in lung airway. It is costly and arduous the comprehensive particle deposition characterization in the total (upper and lower) airway using experimental methods. Therefore, the particle motion numerical simulation in the airway is an efficient method to confront with this problem, and it could indicate the patterns of particle deposition in the whole lung airway. The upper and lower airways are the divisions of the total lung. The model of airway includes of oral cavity (mouth and palate), pharynx, larynx, trachea, B1, B2 and B3. There are resemblance between the human airway model dimensions with a human cast reported by Zhang et al. [18]. As indicated in Figure 1, the glottis to the first carina length and the mouth to the trachea length were near to 14 and 12 cm, respectively [18-19]. Furthermore, 1.60 cm was the trachea diameter. In this model, the airway wall is presumed as smooth and rigid. The cartilaginous rings impacts are not considered appearing in the human airway.

2.2 Governing equations in human airway

In the total lung airway system, some doubts existed for the transition of turbulent flow on the flow rate critical Reynolds number. The approximation of turbulent flow for a flow rate more than 12 L.min$^{-1}$ was reported by Moghadas, et al. seeming rational particularly for track and field as the vibrant activities [20-22]. The Navier-Stokes equations and the continuity equation are dominant equations for the oscillating two-dimensional airflow. Zhang and Kleinstreuer [10] illustrated that it is decent for such internal laminar-to-turbulent flows. Generally, the equations of transport in tensor notation shows indirectly the double-index summation convention [10].

![Figure 1. The model of airway based on the Zhang et al. model. [18, 7].](image-url)
Continuity equation:

\[
\frac{\partial u_i}{\partial x_i} = 0
\]  

(1)

Momentum equation:

\[
\frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_j} = \frac{1}{\rho} \frac{\partial p}{\partial x_i} + \frac{\partial}{\partial x_j} \left[ (\nu + \nu_T) \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) \right]
\]  

(2)

Turbulent kinetic energy (k) equation:

\[
\frac{\partial k}{\partial t} + u_j \frac{\partial k}{\partial x_j} = \tau_{ij} \frac{\partial u_i}{\partial x_j} - \beta^5 k \omega + \frac{\partial}{\partial x_j} \left[ (\nu + \sigma_k \nu_T) \left( \frac{\partial k}{\partial x_j} \right) \right]
\]  

(3)

Pseudo-vorticity (\(\omega\)) equation:

\[
\frac{\partial \omega}{\partial t} + u_j \frac{\partial \omega}{\partial x_j} = \tau_{ij} \alpha \frac{\partial u_i}{\partial x_j} - \beta ^5 \omega \left( \frac{\partial k}{\partial x_j} \right) + \frac{\partial}{\partial x_j} \left[ (\nu + \sigma_\omega \nu_T) \left( \frac{\partial \omega}{\partial x_j} \right) \right]
\]  

(4)

For simplicity, summation sign is used with \(i, j = 1, 2\) where the \(x, y\) components of the velocity and the spatial coordinate vector are \(u_1, u_2\) and \(x_1, x_2\), respectively. Time, density, pressure, kinetic energy, and dissipation per unit turbulence kinetic energy are the \(t, \rho, p, \nu, T\), and \(\omega\), respectively. The turbulent viscosity, \(\nu_T\) is given as \(\nu_T = k \nu_f / \omega\), and the function \(f_\mu = \exp[-3.4/(1 + R_T/50)^2]\) with \(R_T = \rho k / (\omega \mu)\) while \(\mu\) is the dynamic molecular viscosity (\(\mu = \rho \nu\)). \(c_\mu, \alpha, \beta, \beta^*, \sigma_k, \) and \(\sigma_\omega\) are turbulence constants, i.e., \(c_\mu = 0.09, \alpha = 0.555, \beta = 0.8333, \beta^* = 1, \sigma_k = \sigma_\omega = 0.5\).

The primary values in inlet of \(k\) and \(\omega\) are calculated by [10]:

\[
k_{in} = 1.5 \ (I \times P_{in}) \ , \ \omega_{in} = \frac{k_{in}^{0.5}}{0.6 \pi}
\]  

(5)

Where the turbulence intensity and the radius of inlet tube are \(I\) and \(R\), respectively. The convection–diffusion mass transfer equation of nano-particles, where the dominant transfer mechanisms are Brownian motion and turbulent dispersion, can be written as

\[
\frac{\partial Y}{\partial t} + u_j \frac{\partial Y}{\partial x_j} = \frac{\partial}{\partial x_i} \left[ (\bar{D} + \frac{\nu_T}{\sigma_Y}) \frac{\partial Y}{\partial x_i} \right]
\]  

(6)

Where \(\bar{D}\) is the molecular diffusivity of the cigarette smoke. The diffusivity in cigarette smoke is not very significant from compound to compound [17]. \(Y_{in}=0\) is the boundary condition at the wall regarding that a perfect sink for aerosols or vapours on touch is the airway wall. This idea is rational for fast gas-wall reaction kinetics, or vapours of high solubility and reactivity, as well as appropriate for estimating the maximum deposition of vapours in the airways. The aerosol diffusion coefficient is calculated as follows [23, 24]:

\[
\bar{D}_p = \frac{(k_B T C_{slip})}{(3 \pi \eta D_p)}
\]  

(7)

Where \(T\) is the cigarette smoke temperature, \(k_B\) is the Boltzmann constant \((1.38 \times 10^{-23} \text{J/K}^{-1})\), \(D_p\) is the particle diameter and \(C_{slip}\) is the Cunningham slip correction factor [25]:

\[
C_{slip} = 1 + \frac{2 \lambda_m}{D_p} \left[ 1.142 + 0.058 \exp\left( -0.999 \frac{D_p}{2 \lambda_m} \right) \right]
\]  

(8)

where \(\lambda_m\) is the air mean free path. The nanoparticles local wall mass flux could be calculated as [10]

\[
m_w = -\rho A_i \left( \bar{D} + \frac{\nu_T}{\sigma_Y} \right) \frac{\partial Y}{\partial n_i}
\]  

(9)

Where the area of local wall cell \(i\) is \(A_i\), and the direction normal to the wall is \(n\). The local deposition fraction (DF) of nano-particles, defining as the ratio of local wall mass flux to the inlet mass flux, expressed as

\[
DF_{local} = \left[ -\rho A_i \left( \bar{D} + \frac{\nu_T}{\sigma_Y} \right) \frac{\partial Y}{\partial n_i} \right]/(Q_{in} Y_{in})
\]  

(10)

and the regional DF can be determined as

\[
DF_{region} = \sum_{i=1}^{n_{wall}} A_i \left( \bar{D} + \frac{\nu_T}{\sigma_Y} \right) \frac{\partial Y}{\partial n_i} / (Q_{in} Y_{in})
\]  

(11)

Where the number of wall cells in one particular airway area is \(n_{wall}\), e.g., oral airway, first airway bifurcation, etc., as well as the flow rate and mass fraction at the mouth are \(Q_{in}\) and \(Y_{in}\), respectively. The regional deposition fraction could be calculated based on the Fick’s law [7]. The model are used for a range of flow rates from 30 L/min to 80 L/min, corresponding to inlet mean velocities of 0.9417 m/s to 2.354 m/s, particle inlet velocities from 5.1 m/s to 8.4 m/s, and varying particle diameters from 1 nm to 100 nm. \(T_{wall} = 310 \text{ K}\). Also boundary condition no slip at the wall and Pharynx and larynx wall are rigid.

### 3.1 Characteristics of velocity structures

Selected cross sections of the 1-2 models, Profile flows, in the mouth and trachea, are displayed in figures 2a that velocity is fully develop, and 2b figures show the velocity profile for mouth and trachea at an inhalation flow rate of 60 L/min. The glottis, one of the cross-sectional areas is less than other ones of the human airway. Thus, the difference of cross-sectional areas results in the resistance against increment in various flow rates. This resistance created against the air flow decreases the mean velocity. As shown in these figures, the central part of velocity profile is higher than the edges. The velocity of flow varies from a minimum on walls to a maximum in mouth and trachea section.
3.2 Nano-particle deposition

The deposition fraction versus the nano-particle diameters for different rates of cigarette smoking is depicted in the Figure 3. As shown, the deposition of particle decreases with the diameter increment. The concentration of particle in cigarette smoke is totally high (~10^{12} particles in one cigarette). Moreover, the hygroscopic nature of the smoke droplets leads to rapid changes in diameter of particle through condensation and coagulation [26]. Gravitational sedimentation, inertial impaction and Brownian motion (diffusion) are the three basic mechanisms that influence on the behaviour of particles in cigarette smoke within the respiratory tract. ‘Aerodynamic’ effects such as sedimentation and impaction are the important ones. They increase with size increment. Although aerodynamic impacts are negligible for particles of significantly small size, thermodynamic effects are negligible for large particles. The smoke particle deposition lies on the particle size which may vary because of the high relative-humidity condition in the respiratory tract. Although the diameter of the smoke particles is small, 60–80% efficiencies of smoke deposition in the lung have been reported [27]. Upon the high flow rate, the nano-particles are interlocked. Because of the weight increment, they deposit on airway walls. Thus, through flow rate increment, the deposition of particle decreases. Accordingly, the inhalation of cigarette smoke nano-particles in low-flow rate could results in more damage in the lung airway. The results of particle deposition in different flow rate are in good agreement with the simulation results reported by Zang and Kleinsrteuer [17].

Figure 4 indicates the selected four vapour deposition fractions of cigarette smoke in the human airways, which incorporate the representative wall absorption conditions. In this case, steady puffing with inspiratory is obtained in different flow rates from 30 to 80 L/min. During puffing (3 sec), the soft palate (or glottis) is closed for most smokers; however, some smokers, directly, inhale the aerosols in to the lung [28]. In this study, steady puffing inhalation refers to the latter (presumably worst) case, so that the aerosols are assumed to be inhaled directly in to the lung. Clearly, the impact of airway wall absorption (or vapor solubility) can be vital for vapor deposition in human airways. The deposition fractions versus the diameter of nano-particle for various cigarette smoking rates are indicated in the Figure 3. As indicated, the deposition of particle decreases with the diameter increment. The nano-particles are interlocked under the flow rates of high values. Moreover, they deposit on walls of the airway because of the weight increment. On the other hand, the deposition of particle decreases with increasing the flow rate. Consequently, the inhalation of harmful nano-particles in the flow rates of low values could result in more damage in the lung airway. As shown in figure 4, the vapor deposition fraction butadiene vapor and carbon monoxide depositions are much lower than those of acrolein and acetaldehyde. Moreover, acrolein and acetaldehyde fully deposit in the upper airways of human from the mouth to generation B3. The deposition of butadiene vapor and carbon monoxide is very low in the upper airways. It is possible that the butadiene vapor and carbon monoxide depositions are much lower than those of acrolein and acetaldehyde.
The local deposition fractions (DFs) for vapors of acetaldehyde and acrolein are shown in Figure 5. The regional deposition for acrolein and acetaldehyde might gradually decrease from the cavity of mouth to bifurcation B3 because of the heavy deposition, leading to lower vapor concentrations at the each inlet of downstream regions. Furthermore, the different airway region surface areas lead to different values of vapor deposition. For instance, while Trachea has the lowest deposition, it receives the highest vapor deposition in the Larynx. The different airway geometries, surface areas, local flow rates and concentrations of inlet vapor are influential and the deposition fractions in individual bifurcations vary as well. Carbon monoxide and butadiene vapor deposition is very low in the airway model from the oral cavity to generation B3.

The concentration distribution of nano-particles (dp = 5 nm) in the upper airway model for the cigarette smoke vapors flow rate of 60 L/min during cyclic inhalation have been indicated in the figure 6. As indicated, the airway edges concentration profile is higher than airway center. Because of the less soluble vapors such as cigarette smoke the wall concentration would be greater than zero so that mass transport in center and in airways must be considered simultaneously when simulating vapor uptake. The most concentration distribution is in the palate, pharynx and larynx section. Because of the nano-particle deposition in the airway length, this distribution of concentration reduces slowly. The mass transfer occurs often in the mouth and palate (oral airway). Therefore, the inhalation of cigarette smoke vapors creates the more damage on the oral airway and B3 section.

The impacts of Reynolds number on Sherwood number in simulation data for cigarette smoke have been indicated in the figure 7. The Sh number, representing the ratio of convective to diffusive mass transport, can be expressed as:

$$Sh = \left( \frac{h_m D}{D_p} \right) \quad (12)$$

Where the airway segment characteristic diameter is D. Thus, obtaining $h_m$, the respiratory coefficient of mass transfer is vital in forecasting the vapours regional deposition accurately. The coefficient of mass transfer in terms of non-dimensional Sh number is a function of Schmidt number (Sc) and Re number, traditionally. It was developed a set of generalized Sh=f (Re, Sc) equations in respect to a model of human airway for flow rates of normal inspiratory by Zhang & Kleinstreuer [29]. However, they were partly idealized. It is noteworthy that these correlations are for constant flows and the values of realistic deposition could be deduced based on constant matching flows with corrections of time delay. The correlation curves of the Sh-Re_local have been indicated in the figure 7. They were simulated for cigarette smoke vapor. Moreover, the convection contribution impact (Re-number) on mass transfer could be observed in the figure 7.
The diameter of local equivalent computed is $D_a$ as
$$ D_a = \left( \frac{4A_l}{\pi} \right)^{1/2}, $$
where average cross-sectional area is $A_l$, and $Re = \frac{4flr}{\rho u D_a}$, where $flr$ is the local flow rate at peak inspiration. Figure 7 shows the effects of Re number on Sh number in simulation data for cigarette smoke. The Re number increment results to increase in the nano-particles turbulent motion, on the other hand, the stronger the convection (Re numbers) is, the higher the mass transfer. Furthermore, the flow structures and airway geometric features influence a lot on cigarette smoke mass transport. Particularly, due to the interactions among local geometric features, flow turbulence and upstream deposition, the Sh=$Sh$ (Re) relationship may be different at various airway areas. The occurrence of upstream turbulent flows may affect both the inlet velocity and particle profiles which enter the bifurcation and could increase deposition within the model.

3. Conclusion

The mass transfer and deposition of cigarette smoke inside the human airway are investigated by the finite element method in this research. That is to say, the mass transfer and deposition of four selected tobacco-smoke vapors, acetaldehyde, acrolein, 1, 3-butadiene and carbon monoxide, in a human airway model under puffing as well as constant flow conditions have been simulated. The deposition of butadiene vapor and carbon monoxide gas is negligible in comparison to acrolein and acetaldehyde in the total human airways from mouth to generation B3. The deposition of particle decreased with increasing the diameter illustrated by the results. Moreover, the particle deposition decreased with the flowrate increment. The concentration profile of the airway edges was higher than the airway center. This distribution of concentration reduced slowly because of the nano-particle deposition in airway length apart from B3. Moreover, the results illustrate that deposition of cigarette smoking vapor in the upper airway is more than the lower airway. The results are likely to enhance assessing the level of cigarette-smoke damage in the total lung airway.

### References


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